Homework 5 for "Convex Optimization"

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1 Algorithms for ℓ_1 minimization

Consider the ℓ_1 -regularized problem

(1.1)
$$\min_{x} \quad \frac{1}{2} ||Ax - b||_{2}^{2} + \mu ||x||_{1},$$

where $A \in \mathbb{R}^{m \times n}$, $b \in \mathbb{R}^m$ and $\mu > 0$ are given. Test matrices:

```
n = 1024;
m = 512;
A = randn(m,n);
u = sprandn(n,1,0.1);
b = A*u;
mu = 1e-3;
```

See http://bicmr.pku.edu.cn/~wenzw/courses/Test_l1_regularized_problems.m

- 1. Solve (1.1) using CVX by calling different solvers mosek and gurobi.
- 2. Solve (1.1) by calling mosek and gurobi directly.
- 3. Write down and implement three of the following algorithms in Matlab:
 - (a) Projection gradient method by reformulating the primal problem as a quadratic program with box constraints
 - (b) Subgradient method for the primal problem
 - (c) Gradient method for the smoothed primal problem
 - (d) Fast gradient method for the smoothed primal problem
 - (e) Proximal gradient method for the primal problem
 - (f) Fast proximal gradient method for the primal problem
 - (g) Augmented Lagrangian method for the dual problem
 - (h) Alternating direction method of multipliers for the dual problem
 - (i) Alternating direction method of multipliers with linearization for the primal problem

4. Requirement:

(a) The interface of each method should be written in the following format

```
[x, out] = method_name(x0, A, b, mu, opts);
```

Here, x0 is a given input initial solution, A, b and mu are given data, opts is a struct which stores the options of the algorithm, out is a struct which saves all other output information.

- (b) Compare the efficiency (cpu time) and accuracy (checking optimality condition) in the format as http://bicmr.pku.edu.cn/~wenzw/courses/Test_l1_regularized_problems.m
- (c) Pack all of your codes in one file named as "11-hw-name-ID.zip" and send it to both me and TA: wendouble@gmail.com jiangke1990@gmail.com
- (d) If you get significant help from others on one routine, write down the source of references at the beginning of this routine.